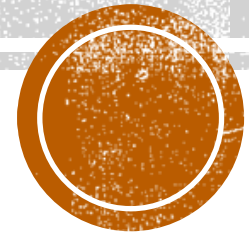


MATH WORKSHOP

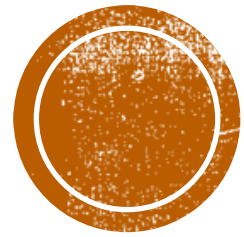
For Parents

8 April 2022



By: Mrs Tay Yuyan





PROBLEM SOLVING



Solving problems to learn math

PROBLEM SOLVING STRATEGIES

R  READ

I IDENTIFY KEYWORDS 

G GET A PLAN 

H HAVE IT DONE 

T TRIPLE CHECK 

MEWAS
odel quation orking nswer tatement

N umber

T ransfer

U nits

C alculatation

PROBLEM SOLVING STRATEGY

READ 

→ **Topic**

IDENTIFY KEYWORDS 

→ **Type of question**

GET A PLAN 

→ **Heuristics**

HAVE IT DONE 

TRIPLE CHECK 

QUESTION 1

PSLE 2017 PAPER 1 Q28 (2 MARKS)

A box contains red, blue and yellow beads. $\frac{1}{4}$ of the beads are red. $\frac{2}{9}$ of the remaining beads are blue. What fraction of the beads in the box are yellow?

Read

Topic

Fractions

Identify keywords

Type of qns

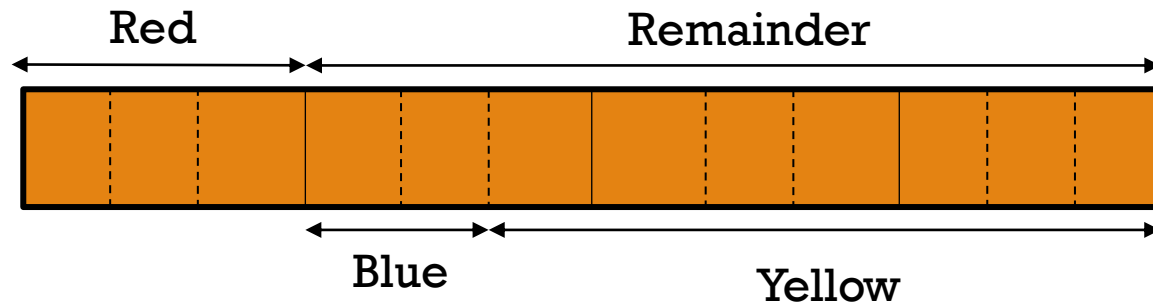
Remainder concept

Get a plan

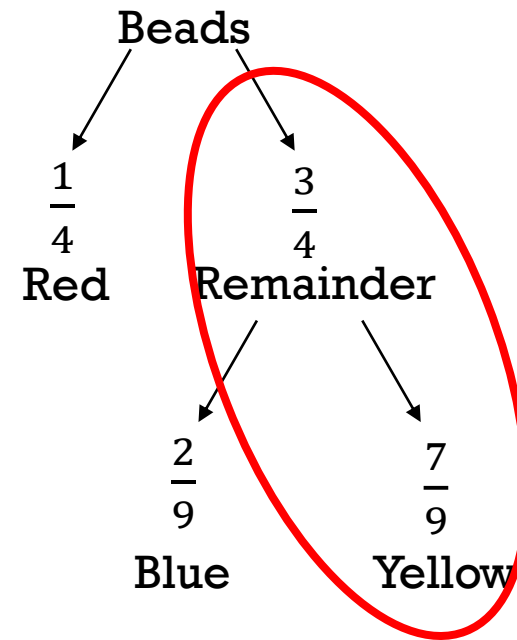
Heuristics

Model / Branching

A box contains red, blue and yellow beads. $\frac{1}{4}$ of the beads are red. $\frac{2}{9}$ of the remaining beads are blue. What fraction of the beads in the box are yellow?



$\frac{7}{12}$ of the beads in the box are yellow.



$$\frac{7}{9} \times \frac{3}{4} = \frac{7}{12}$$

$\frac{7}{12}$ of the beads in the box are yellow.

QUESTION 2

PSLE 2020 PAPER 2 Q17 (5 MARKS)

Mrs Wu spent $\frac{1}{6}$ of her money on a dress and 2 blouses. The dress cost 3 times as much as each blouse. Mrs Wu spent $\frac{3}{4}$ of her remaining money on a watch. She spent \$220.50 more on the watch than on the dress.

- (a) What fraction of Mrs Wu's money was spent on each blouse?
- (b) How much money did Mrs Wu have at first?

QUESTION 2

PSLE 2020 PAPER 2 Q17 (5 MARKS)

Mrs Wu spent $\frac{1}{6}$ of her money on a dress and 2 blouses. The dress cost 3 times as much as each blouse. Mrs Wu spent $\frac{3}{4}$ of her remaining money on a watch. She spent \$220.50 more on the watch than on the dress.

Read

Topic

Fractions / Money

Identify keywords

Type of qns

Remainder concept

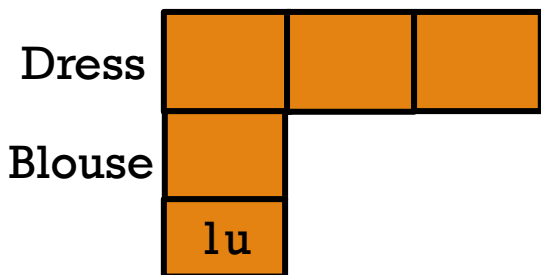
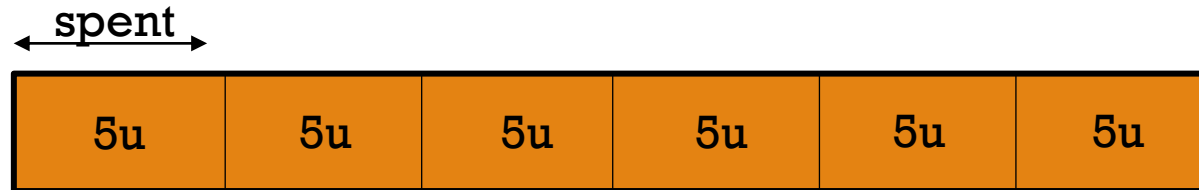
Get a plan

Heuristics

Model / Branching

Mrs Wu spent $\frac{1}{6}$ of her money on a dress and 2 blouses. The dress cost 3 times as much as each blouse. Mrs Wu spent $\frac{3}{4}$ of her remaining money on a watch. She spent \$220.50 more on the watch than on the dress.

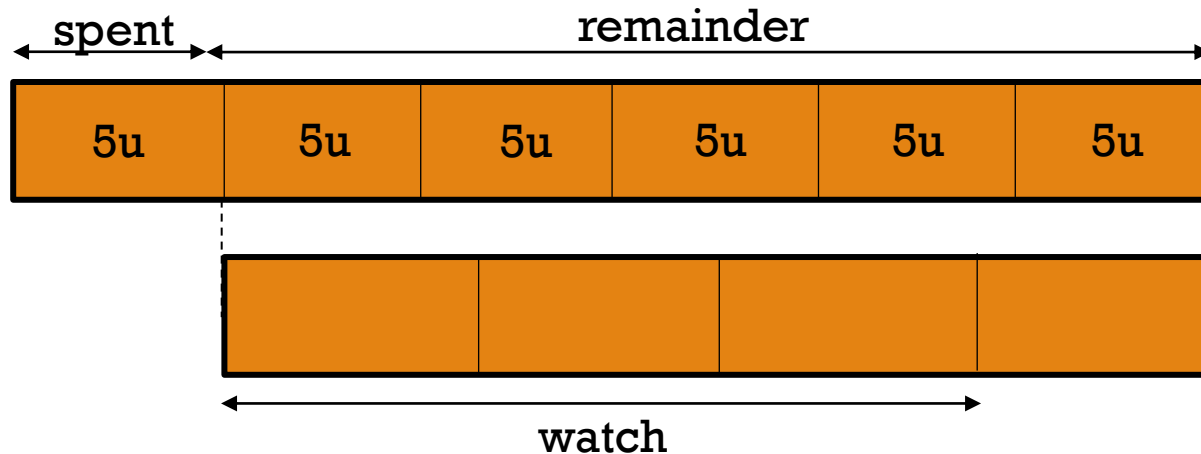
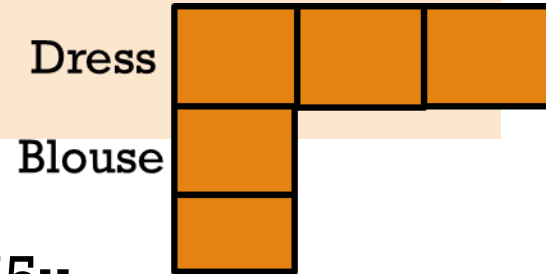
(a) What fraction of Mrs Wu's money was spent on each blouse?



(a) $\frac{1}{30}$ of Mrs Wu's money was spent on each blouse.

Mrs Wu spent $\frac{1}{6}$ of her money on a dress and 2 blouses. The dress cost 3 times as much as each blouse. Mrs Wu spent $\frac{3}{4}$ of her remaining money on a watch. She spent \$220.50 more on the watch than on the dress.

(b) How much money did Mrs Wu have at first?



$$(\text{watch}) \frac{3}{4} \times 25u = 18.75u$$

$$(\text{diff btw watch \& dress}) 18.75u - 3u = 15.75u$$

$$15.75u = \$220.50$$

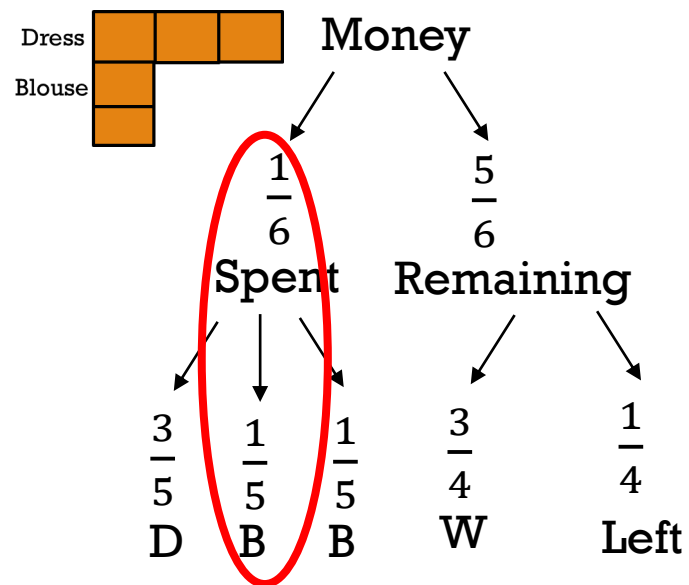
$$1u = \$220.50 \div 15.75 = \$14$$

$$30u = \$14 \times 30 = \$420$$

(b) Mrs Wu had **\$420** at first.

Mrs Wu spent $\frac{1}{6}$ of her money on a dress and 2 blouses. The dress cost 3 times as much as each blouse. Mrs Wu spent $\frac{3}{4}$ of her remaining money on a watch. She spent \$220.50 more on the watch than on the dress.

(a) What fraction of Mrs Wu's money was spent on each blouse?

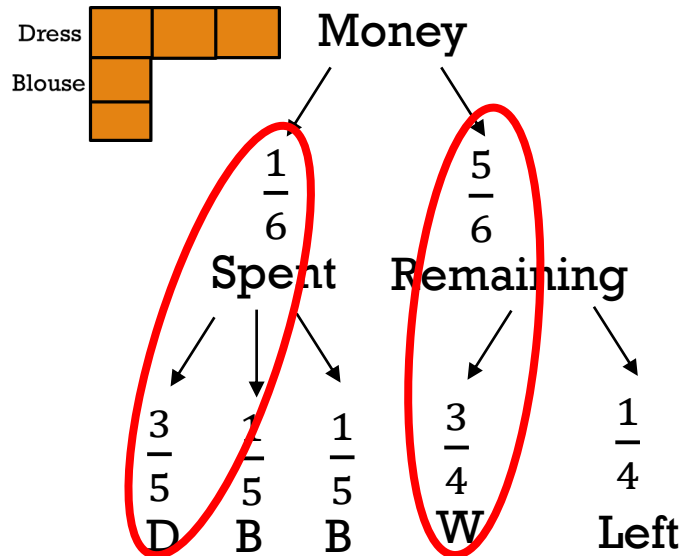


$$\frac{1}{5} \times \frac{1}{6} = \frac{1}{30}$$

(a) $\frac{1}{30}$ of Mrs Wu's money was spent on each blouse.

Mrs Wu spent $\frac{1}{6}$ of her money on a dress and 2 blouses. The dress cost 3 times as much as each blouse. Mrs Wu spent $\frac{3}{4}$ of her remaining money on a watch. She spent \$220.50 more on the watch than on the dress.

(b) How much did Mrs Wu have at first?



$$\text{(dress)} \quad \frac{3}{5} \times \frac{1}{6} = \frac{1}{10}$$

$$\text{(watch)} \quad \frac{3}{4} \times \frac{5}{6} = \frac{5}{8}$$

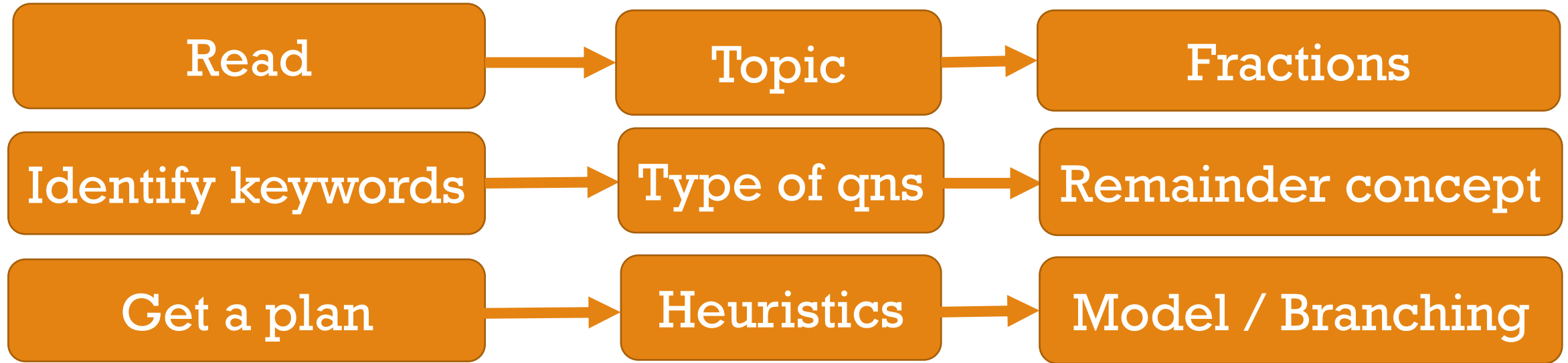
$$\text{(diff btw watch \& dress)} \quad \frac{5}{8} - \frac{1}{10} = \frac{21}{40}$$

$$\frac{21}{40} \text{ of money} = \$220.50$$

$$\frac{1}{40} \text{ of money} = \$220.50 \div 21 = \$10.50$$

$$\frac{40}{40} \text{ of money} = \$10.50 \times 40 = \$420$$

(b) Mrs Wu had \$420 at first.



QUESTION 3

PSLE 2012 PAPER 2 Q4 (2 MARKS)

The ratio of the number of angelfish to that of a clownfish in an aquarium was 5 : 4 at first. After 3 clownfish were sold, the ratio of the number of angelfish to that of clownfish became 4 : 3. What was the total number of clownfish in the aquarium at first?

Read

Topic

Ratio

Identify keywords

Type of qns

Before & After

Get a plan

Heuristics

Restate the problem

What remained unchanged?



QUESTION 4

PSLE 2019 PAPER 2 Q10 (3 MARKS)

At first, the ratio of the number of boys to the number of girls in a chess club was 4 : 1. After 6 boys and 6 girls joined the club, the ratio became 3 : 1.

- (a) Did the percentage of members who are boys increase, decrease or remain the same? Show your working clearly.
- (b) In the end, how many boys were there in the club?

QUESTION 4

PSLE 2019 PAPER 2 Q10 (3 MARKS)

At first, the ratio of the number of boys to the number of girls in a chess club was 4 : 1. After 6 boys and 6 girls joined the club, the ratio became 3 : 1.

Read

Topic

Ratio

Identify keywords

Type of qns

Before & After

Get a plan

Heuristics

Restate the problem

At first, the ratio of the number of boys to the number of girls in a chess club was 4 : 1. After 6 boys and 6 girls joined the club, the ratio became 3 : 1.

(a) Did the percentage of members who are boys increase, decrease or remain the same? Show your working clearly.

What remained unchanged?

	<u>Before</u>			6 boys joined 6 girls joined	<u>After</u>		
	Boys	Girls	Diff		Boys	Girls	Diff
	4	1	3		3	1	2
$\times 2$	8	2	6		9	3	6
	$\frac{8}{10} \times 100\% = 80\%$				$\frac{9}{12} \times 100\% = 75\%$		

(a) The percentage of members who are boys **decreased**.

At first, the ratio of the number of boys to the number of girls in a chess club was 4 : 1. After 6 boys and 6 girls joined the club, the ratio became 3 : 1.

(b) In the end, how many boys were there in the club?

What remained unchanged?

	<u>Before</u>			6 boys joined 6 girls joined	<u>After</u>		
	Boys	Girls	Diff		Boys	Girls	Diff
	4	1	3		3	1	2
$\times 2$	8	2	6		9	3	6

$$1u = 6$$

$$9u = 9 \times 6$$

$$= 54$$

(b) In the end, there were **54** boys in the club.

QUESTION 5

PSLE 2014 PAPER 2 Q13 (3 MARKS)

Mr Lim had a total of 540 long and short rulers. After selling an equal number of both types, he had $\frac{1}{3}$ of the long rulers and $\frac{1}{6}$ of the short ones left. What was the total number of rulers left?

Read

Topic

Fractions

Ratio

Identify keywords

Type of qns

Before & After

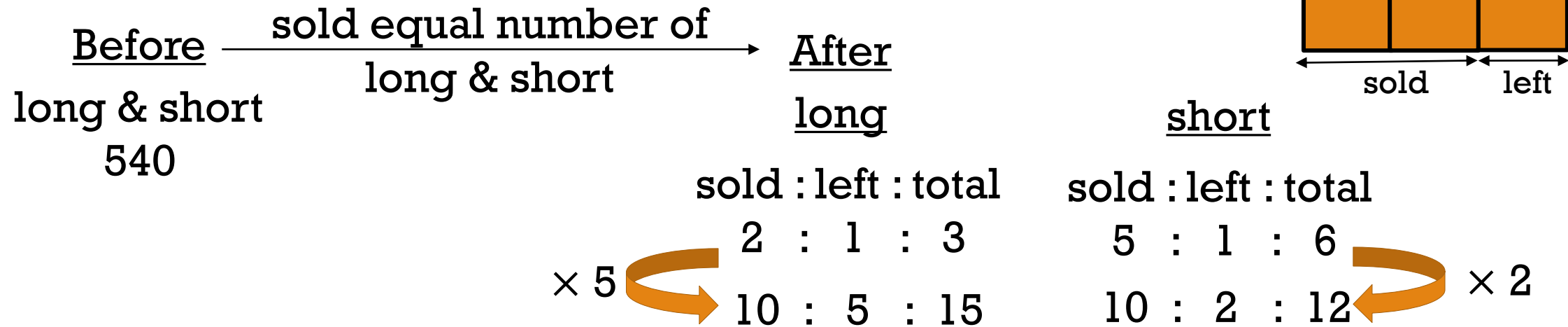
Get a plan

Heuristics

Restate the problem

Mr Lim had a total of 540 long and short rulers. After selling an equal number of both types, he had $\frac{1}{3}$ of the long rulers and $\frac{1}{6}$ of the short ones left. What was the total number of rulers left?

What remained the same?

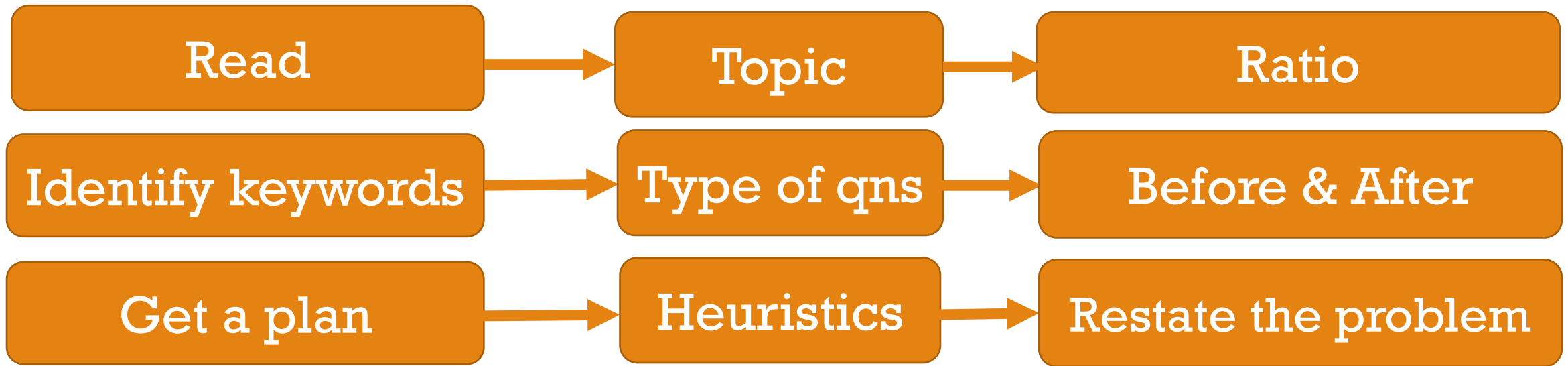


$$27u = 540$$

$$1u = 540 \div 27 = 20$$

$$7u = 7 \times 20 = 140$$

The total number of rulers left was **140**.



What remained unchanged?

What remained the same?

QUESTION 6

PSLE 2017 PAPER 2 Q15 (4 MARKS)

At a walkathon, each participant completed either a 3-km route, a 5-km route or an 8-km route. $\frac{1}{4}$ of the participants completed the 3-km route, $\frac{9}{20}$ of the participants completed the 5-km route and the rest completed the 8-km route. For every 1 km a participant walked, \$4 was donated to charity. A total of \$8208 was donated to charity.

- (a) What is the ratio of the number of participants who completed the 3-km route to the number who completed the 5-km route to the number who completed the 8-km route?
- (b) What is the total number of participants at the walkathon?

QUESTION 6

PSLE 2017 PAPER 2 Q15 (4 MARKS)

At a walkathon, each participant completed either a 3-km route, a 5-km route or an 8-km route. $\frac{1}{4}$ of the participants completed the 3-km route, $\frac{9}{20}$ of the participants completed the 5-km route and the rest completed the 8-km route. For every 1 km a participant walked, \$4 was donated to charity. A total of \$8208 was donated to charity.

Read

Topic

Fractions

Identify keywords

Type of qns

Number x Value

Get a plan

Heuristics

Make a table

At a walkathon, each participant completed either a 3-km route, a 5-km route or an 8-km route. $\frac{1}{4}$ of the participants completed the 3-km route, $\frac{9}{20}$ of the participants completed the 5-km route and the rest completed the 8-km route. For every 1 km a participant walked, \$4 was donated to charity. A total of \$8208 was donated to charity.

(a) What is the ratio of the number of participants who completed the 3-km route to the number who completed the 5-km route to the number who completed the 8-km route?

$$\text{3-km route} \rightarrow \frac{1}{4} \text{ of participants} = \frac{5}{20} \text{ of participants}$$

$$\text{5-km route} \rightarrow \frac{9}{20} \text{ of participants}$$

$$\text{8-km route} \rightarrow 1 - \frac{1}{4} - \frac{9}{20} = \frac{6}{20}$$

The ratio is 5 : 9 : 6.

At a walkathon, each participant completed either a 3-km route, a 5-km route or an 8-km route. $\frac{1}{4}$ of the participants completed the 3-km route, $\frac{9}{20}$ of the participants completed the 5-km route and the rest completed the 8-km route. For every 1 km a participant walked, \$4 was donated to charity. A total of \$8208 was donated to charity.
 (b) What is the total number of participants at the walkathon?

	Number (No. of participants)	Value (Distance)	Total (Total distance)
3-km route	5u	1 participant = 3 km	5 x 3 km = 15 km
5-km route	9u	1 participant = 5 km	9 x 5 km = 45 km
8-km route	6u	1 participant = 8 km	6 x 8 km = 48 km

1 group
 (No. of participants) $5 + 9 + 6 = 20$
 (Dist walked) $15 + 45 + 48 = 108$

(Dist walked by all participants) $\$8208 \div \$4 = 2052$

(No. of groups) $2052 \div 108 = 19$

(Total no. of participants) $19 \times 20 = 380$

The total number of participants at the walkathon is **380**.

QUESTION 7

PSLE 2020 PAPER 2 Q14 (3 MARKS)

Andy saved a total of \$108 in coins in his coin box. $\frac{2}{3}$ of the coins saved were one-dollar coins. There were 3 times as many one-dollar coins as fifty-cent coins. The remaining coins were twenty-cent coins. How many coins did Andy save in the coin box altogether?

Read

Topic

Fractions / Ratio

Identify keywords

Type of qns

Number x Value

Get a plan

Heuristics

Make a table

Andy saved a total of \$108 in coins in his coin box. $\frac{2}{3}$ of the coins saved were one-dollar coins. There were 3 times as many one-dollar coins as fifty-cent coins. The remaining coins were twenty-cent coins. How many coins did Andy save in the coin box altogether?

$$\begin{array}{lcl}
 \$1 \text{ coins} : 50\text{-cent} \text{ \& } 20\text{-cent coins} : \text{total} & & \$1 \text{ coins} : 50\text{-cent coins} \\
 \times 3 \quad \begin{array}{c} \curvearrowright \\ 2 : 1 : 3 \\ \curvearrowleft \\ 6 : 3 : 9 \end{array} & & \begin{array}{c} 3 : 1 \\ 6 : 2 \end{array} \quad \begin{array}{c} \curvearrowright \\ \times 2 \\ \curvearrowleft \end{array}
 \end{array}$$

$$\begin{array}{lcl}
 \$1 \text{ coins} : 50\text{-cent coins} : 20\text{-cent coins} \\
 6 : 2 : 1
 \end{array}$$

	Number (No. of coins)	Value (Value of coins)	Total (Total value)
\$1 coins	6u	1 coin = \$1	6 x \$1 = \$6
50-cent coins	2u	1 coin = 50¢	2 x 50¢ = \$1
20-cent coins	1u	1 coin = 20¢	1 x 20¢ = \$0.20

$$\begin{array}{l}
 \underline{1 \text{ group}} \\
 (\text{No. of coins}) \quad 6 + 2 + 1 = 9 \\
 (\text{Value of coins}) \quad \$6 + \$1 + \$0.20 \\
 \quad \quad \quad = \$7.20
 \end{array}$$

$$\begin{array}{l}
 (\text{No. of groups}) \quad \$108 \div \$7.20 = 15 \\
 (\text{Total no. of coins}) \quad 15 \times 9 = 135
 \end{array}$$

Andy saved **135** coins in the coin box altogether.

QUESTION 8

PSLE 2021 PAPER 2 Q14 (4 MARKS)

The table shows the prices of tickets for a concert.

Type	Age	Price per ticket
Adult	Below 60 years	\$16
	60 years and above	\$11
Child	Below 16 years	\$7

The number of adult tickets sold was 5 times the number of child tickets sold. $\frac{5}{8}$ of the adult tickets sold were for adults aged below 60 years. A total of \$5589 was collected from the sale of tickets.

- (a) What fraction of the tickets sold were for adults aged 60 years and above?
- (b) What was the total number of tickets sold?

The table shows the prices of tickets for a concert.

Type	Age	Price per ticket
Adult	Below 60 years	\$16
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The number of adult tickets sold was 5 times the number of child tickets sold. $\frac{5}{8}$ of the adult tickets sold were for adults aged below 60 years. A total of \$5589 was collected from the sale of tickets.

Read

Topic

Fractions / Ratio

Identify keywords

Type of qns

Number x Value

Get a plan

Heuristics

Make a table

The table shows the prices of tickets for a concert.

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Child	Below 16 years	\$7

The number of adult tickets sold was 5 times the number of child tickets sold. $\frac{5}{8}$ of the adult tickets sold were for adults aged below 60 years. A total of \$5589 was collected from the sale of tickets.

(a) What fraction of the tickets sold were for adults aged 60 years and above?

adult : child

5 : 1

$\times 8$ 40 : 8

Below 60 : 60 & above : adults

5 : 3 : 8

25 : 15 : 40

$\times 5$

$\frac{15}{48} = \frac{5}{16}$

Below 60 : 60 & above : child : total

25 : 15 : 8 : 48

(a) $\frac{5}{16}$ of the tickets sold were for adults aged 60 and above.

The table shows the prices of tickets for a concert.

Type	Age	Price per ticket
Adult	Below 60 years	\$16
	60 years and above	\$11
Child	Below 16 years	\$7

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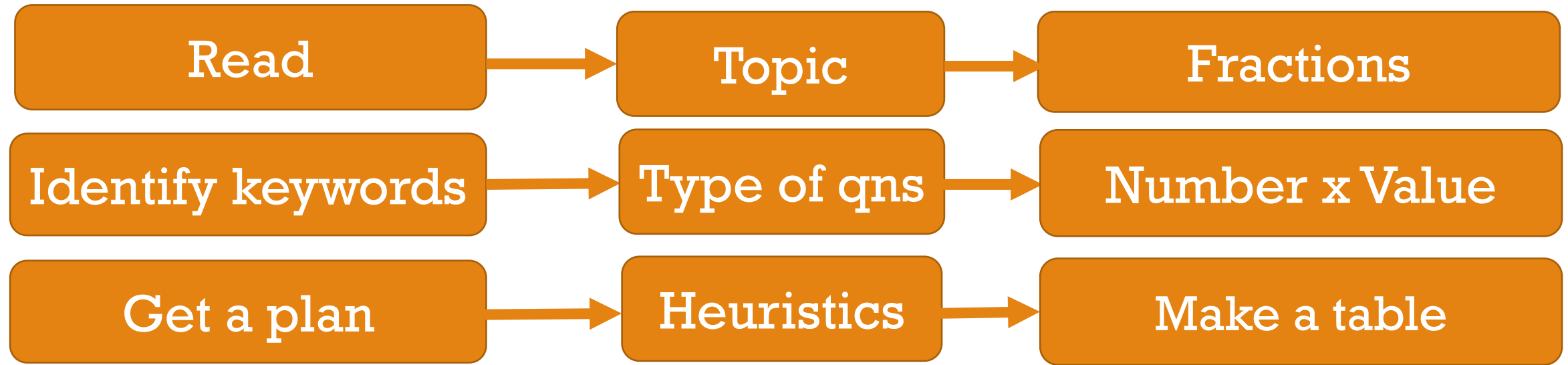
(b) What was the total number of tickets sold?

	Number (No. of tic)	Value (Value of tic)	Total (Total value)
Below 60	25u	1 ticket = \$16	25 x \$16 = \$400
60 & above	15u	1 ticket = \$11	15 x \$11 = \$165
Child	8u	1 ticket = \$7	8 x \$7 = \$56

$$\begin{aligned}
 &\text{1 group} \\
 &(\text{No. of tic}) 25 + 15 + 8 = 48 \\
 &(\text{Value of tic}) \$400 + \$165 + \$56 \\
 &= \$621
 \end{aligned}$$

$$\begin{aligned}
 &(\text{No. of groups}) \$5589 \div \$621 = 9 \\
 &(\text{Total no. of tic}) 9 \times 48 = 432
 \end{aligned}$$

The total number of tickets sold was **432**.



PROBLEM SOLVING STRATEGIES

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I IDENTIFY KEYWORDS 

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T TRIPLE CHECK 

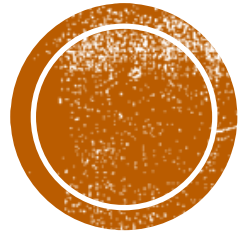
MEWAS
odel quation orking nswer tatement

N umber

T ransfer

U nits

C alculatation



MATH AROUND US



Learning math to solve problems

solving problems
to learn math

learning math
to solve problems

Thank You!

